

End Semester Examination September/ October 2015  
Year I Semester I

Mathematics for Biological Sciences (EAG 101-1)

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**Instructions to Candidates**

Answer **All** questions.

No. of questions : Two (02)

No. of pages : Two (02)

Total marks allocated : 100%

Time : One (01) hour

Use standard symbols without definition.

Scientific calculators are allowed.

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**Question 1**

1.1 Draw the graph of the following function.

$$f(x) = \begin{cases} 9 - x; & \text{if } x \leq 2 \\ x^2 - 2; & \text{if } x > 2 \end{cases}$$

(10 marks)

1.2 A closed cylindrical "Can" has a surface area  $120\pi \text{ cm}^2$ . Express the volume of the "Can" as a function of its radius  $r$ .

(10 marks)

1.3 Find each of the following limits.

a)  $\lim_{x \rightarrow 2} 3x^2 - 5x + 2$

(5 marks)

b)  $\lim_{x \rightarrow 2} \frac{x^2 - 4}{x^2 + 5x + 6}$

(5 marks)

c)  $\lim_{x \rightarrow \infty} \frac{x^3 + x - 3}{3 - 2x - 3x^3}$

(5 marks)



1.4 Simplify the following expression.

$$\left(\frac{2x^2y^0z^{-5}}{14y^{-1}xz^3}\right)$$

(8 marks)

1.5 Expand the following expression.

$$\log_7(x^2\sqrt{1-y^2})$$

(7 marks)

## Question 2

2.1 Find the derivative of the following function using the standard definition.

$$f(x) = 2x^2 + 5$$

(10 marks)

2.2 Find the derivative of functions given below with respect to  $x$ .

a)  $y = x^3 \cos 2x$

(5 marks)

b)  $y = \frac{x^2+3x+5}{x+1}$

(5 marks)

c)  $y = e^x \ln x$

(5 marks)

2.3 Integrate the following functions with respect to  $x$ .

a)  $\int \left(\frac{2x+1}{2x^2+2x+3}\right) dx$

(5 marks)

b)  $\int (\sin 3x + 5e^{5x} + x^3) dx$

(5 marks)

c)  $\int (2x - 1)^4 dx$

(5 marks)

2.4 Find the value of,  $\int_0^{\pi/2} (\sin x + \cos 2x) dx$ .

(10 marks)